

## Things you should know from 12.1, 2, 3:

### 12.1

- How do you determine the domain of a function  $f(t)$ ? A vector-valued function  $\mathbf{F}(t)$ ?
- How do you sketch an arbitrary curve in 3-space? Some hints:
  - Determine where the curve *begins* and *ends*.
  - Determine what the function looks like in the  $xy$ -,  $xz$ -, and  $yz$ -planes.
  - Know the parametric forms of some basic curves: circle, spiral, expanding / contracting spiral, line.
  - Practice! (And check your answer using MATLAB.)
- How do you determine where a curve intersects a surface?

### 12.2

- How do you compute the limit of a vector valued-function, namely  $\lim_{t \rightarrow t_0} \mathbf{F}(t)$ ? Or, what do I mean by ‘pass the limit inside the vector-valued function’?
- Some basic limit tricks:
  - Plug-in (when you can).
  - L’Hopital’s rule.
  - Factoring numerators and denominators of rational functions.
  - Algebra. (Think of the  $\lim_{t \rightarrow 0} e^{-1/t^2}$  example.)
- When does a limit exist<sup>1</sup>? Must  $\lim_{t \rightarrow t_0} \mathbf{F}(t) = \mathbf{F}(t_0)$ ?
- Basic limit results from Theorem 12.5<sup>2</sup>.

### 12.3

- Basic derivative results: power rule, product rule, quotient rule, chain rule.
- Derivatives of the basic trigonometric functions, exponentials, logarithms.
- Basic antiderivative (integration) results:  $u$ -substitution, integration by parts, the Fundamental Theorem of Calculus.
- How do you compute the derivative of a vector-valued function,  $\frac{d}{dt} \mathbf{F}(t)$ ?

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<sup>1</sup>At least intuitively. Don’t worry about  $\epsilon/\delta$ -style arguments for this quiz.

<sup>2</sup>Though most of these are results you would have guessed without a theorem.

- How do you compute the antiderivative (integral) of a vector-valued function,  $\int \mathbf{F}(t) dt$ ?
- Basic derivative results from Theorem 12.10.
- Given a position vector  $\mathbf{r}(t)$  for some particle in space, how do we compute its velocity  $\mathbf{v}(t)$ ? Speed  $\|\mathbf{v}(t)\|$ ? Acceleration  $\mathbf{a}(t)$ ?
- Given the acceleration vector  $\mathbf{a}(t)$  for a particle in space and its initial position and velocity, how do we compute its velocity  $\mathbf{v}(t)$ ? Position  $\mathbf{r}(t)$ ?